

Topic: Arc Length

Things to remember:

- ✓ Circumference = $2\pi r$
- ✓ r = radius
- ✓ $\frac{\text{arc length}}{\text{circumference } (2\pi r)} = \frac{\text{angle}}{360^\circ}$

Examples:

1. Find the circumference, **in terms of pi**, given the diameter is 14 feet. $r = \frac{14}{2} = 7$

$$C = 2\pi(7)$$

$$C = 14\pi \text{ ft}$$

2. Find the radius given the circumference is 25π in.

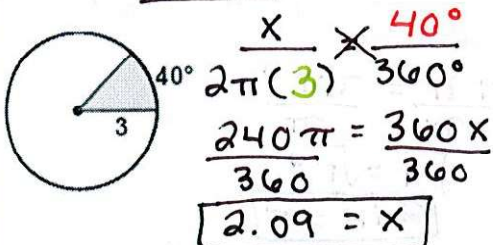
$$C = 2\pi r$$

$$25\pi = 2\pi r$$

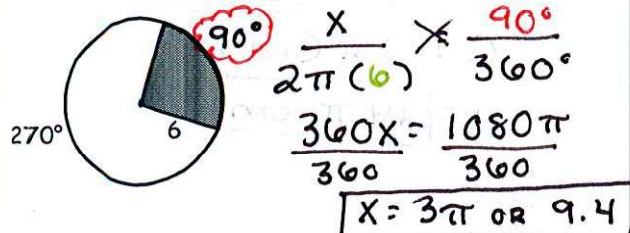
$$\frac{25\pi}{2\pi} = \frac{2\pi r}{2\pi}$$

$$12.5 \text{ in} = r$$

3. Find the arc length of the shaded section.



4. Find the arc length of the **shaded section** *



5. A golf club is swung around to hit a golf ball that created a distance of 15 feet around. If the golf club is 3.67 feet, what was the angle?

$$\frac{15}{2\pi(3.67)} = \frac{X}{360^\circ}$$

$$\frac{23.06X}{23.06} = \frac{5400}{23.06}$$

$$X = 234.17^\circ$$

6. If it's 4 o'clock on the classroom clock and the distance the hour hand has traveled is 12.57 in, what is the length of the hour hand (radius)?

$$\frac{12.57}{2\pi X} = \frac{120^\circ}{360^\circ}$$

$$\frac{240\pi X}{(240\pi)} = \frac{4525.2}{(240\pi)}$$

$$X = 6 \text{ in}$$

Topic: Sector Area

Things to Remember:

- ✓ Area = πr^2
- ✓ $\frac{\text{sector area}}{\text{Area } (\pi r^2)} = \frac{\text{angle}}{360^\circ}$

Examples:

7. Find the area, **in terms of pi**, given the radius is 14 feet.

$$A = \pi(14)^2$$

$$A = 196\pi \text{ ft}^2$$

8. Find the diameter given the area is 25π in.

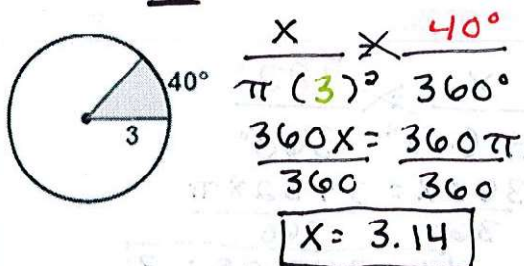
$$A = \pi r^2$$

$$\frac{25\pi}{\pi} = \frac{\pi r^2}{\pi}$$

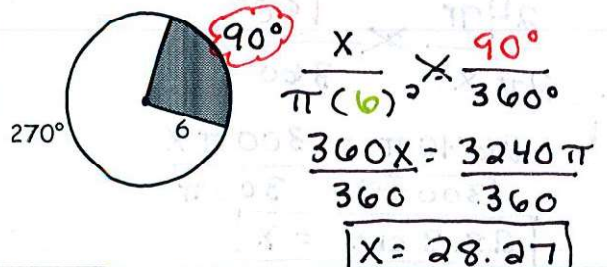
$$\sqrt{25} = \sqrt{r^2}$$

$$5 \text{ in} = r \rightarrow 10 \text{ in} = d$$

9. Find the area of the shaded section.



10. Find the area of the **shaded section**



11. The area of one piece of pizza is $9\pi \text{ in}^2$. The pizza is cut into eighths (**HINT: Find the angle measure using a similar the method we did for the clock**). Find the radius of the pizza pie.

$$\frac{360^\circ}{8} = 45^\circ$$

$$\frac{9\pi}{\pi x^2} \times \frac{45^\circ}{360^\circ}$$

$$\frac{45\pi x^2}{45\pi} = \frac{3240\pi}{45\pi}$$

$$\sqrt{x^2} = \sqrt{72}$$

$$x = 8.49 \text{ in}$$

12. A sprinkler system can shoot water out a distance of 6 yards. If the sprinkler system can cover an area of 75.4 yds^2 , then what angle is the sprinkler system using?

$$\frac{75.4}{\pi (6)^2} \times \frac{x}{360^\circ}$$

$$\frac{36\pi x}{36\pi} = \frac{27144}{(36\pi)}$$

$$x = 240^\circ$$

Mixed Review

13. Find the circumference, in terms of pi, of a circle with a radius of 12 cm.

$$C = 2\pi(12)$$

$$= 24\pi \text{ cm}$$

14. Calculate the radius of a circle that has an area of $4\pi \text{ in}^2$. **Round to the nearest hundredths.**

$$\frac{4\pi}{\pi} = \frac{\pi r^2}{\pi}$$

$$\sqrt{4} = \sqrt{r^2}$$

$$2 \text{ in} = r$$

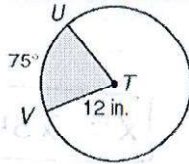
15. What is the area of a 30° sector of a circle with a radius of 5.5 inches?

$$\frac{x}{\pi (5.5)^2} \times \frac{30^\circ}{360^\circ}$$

$$\frac{360x}{360} = \frac{2851}{360}$$

$$x = 7.9 \text{ in}^2$$

16. Find the arc length of the shaded sector. **Round to the nearest hundredths.**



$$\frac{x}{2\pi(12)} \times \frac{75^\circ}{360^\circ}$$

$$\frac{360x}{360} = \frac{1800\pi}{360}$$

$$x = 15.71 \text{ in}$$

17. Find the central angle of a sector that has a length of $15\pi \text{ mm}$ and a radius of 18 mm. **Round to the nearest hundredths.**

$$\frac{15\pi}{2\pi(18)} \times \frac{x}{360^\circ}$$

$$\frac{5400\pi}{36\pi} = \frac{36\pi x}{36\pi}$$

$$x = 150^\circ$$

18. Find the central angle of a sector that has an area of 23 km^2 and a diameter of 10 km. $r = 5$. **Round to the nearest hundredths.**

$$\frac{23}{\pi (5)^2} \times \frac{x}{360^\circ}$$

$$\frac{8280}{(25\pi)} = \frac{25\pi x}{25\pi}$$

$$x = 105.4^\circ$$

19. If the length of a sector is $24\pi \text{ cm}$ and its central angle measure is 150° , what is radius of the circle? **Round to the nearest hundredths.**

$$\frac{24\pi}{2\pi x} \times \frac{150^\circ}{360^\circ}$$

$$\frac{8640\pi}{(300\pi)} = \frac{300\pi x}{300\pi}$$

$$28.8 \text{ cm} = x$$

20. A windshield wiper blade is 18 inches long. To the nearest square inch, what is the area covered by the blade as it rotates through an angle of 122° ? **Round to the nearest hundredths.**

$$\frac{x}{\pi (18)^2} \times \frac{122^\circ}{360^\circ}$$

$$\frac{360x}{360} = \frac{39528\pi}{360}$$

$$x = 344.95 \text{ in}^2$$